



Studybeesofficial

Where Minds Pollinate

Class 11
Mathematics
Chapter 5
Exercise 5.1
Notes

National Book Foundation

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Exercise 5.1

Q1

(i) $2x^3 + 3x^2 - 4x + 1$ is $\div$ by $x+2$.
put $x = -2$

$$P(-2) = 2(-2)^3 + 3(-2)^2 - 4(-2) + 1$$

$$P(-2) = 5$$

which is required remainder

(ii) $x^4 + 2x^3 - x^2 + 2x + 3$ is $\div$ by $x-2$

put $x = 2$

$$P(2) = (2)^4 + 2(2)^3 - (2)^2 + 2(2) + 3$$

$$P(2) = 35$$

which is required remainder.

(Q2) Sol:- put $x = 3$ &

$$P(x) = x^3 - 2x^2 - 5x + 6$$

$$P(3) = (3)^3 - 2(3)^2 - 5(3) + 6$$
$$= 0$$

so $(x-3)$ is a factor

Q3) Sol: $x = 3$

$$P(x) = x^3 - 2x^2 - 5x + 1$$

$$P(3) = (3)^3 - 2(3)^2 - 5(3) + 1$$
$$= -5$$

so $P(3) \neq 0$ so

$(x-3)$ is not a factor

Q4 Sol:- let $D = 4y^3 - 4y^2 + 2y + 10$, $r = 0$
 $q = 4y^2 - 8y + 10$

$q \times d + r = D \Rightarrow q \times d + 0 = D \therefore r = 0$

so $d = \frac{\text{Divident}}{\text{quotient}}$

$4y^2 - 8y + 10 \overline{) 4y^3 - 4y^2 + 2y + 10}$
 $\underline{+ 4y^3 - 8y^2 + 10y}$
 $\quad \quad \quad 10y^2 - 8y + 10$

$4y^2 - 8y + 10$
 $\underline{+ 4y^2 - 8y + 10}$
 $\quad \quad \quad 0$

Hence other factor is $y + 1$

Q5) $P(x) = x^3 + qx^2 - 7x + 6$

put $x = -1$

$(-1)^3 + q(-1)^2 - 7(-1) + 6 = 0$

$-1 + q + 7 + 6 = 0$

$q + 12 = 0$

$q = -12$ Ans

Q6) $P(x) = 2x^3 + 3x^2 - 3x - m$

$x = 2$

Given $P(2) = 16$

$2(2)^3 + 3(2)^2 - 3(2) - m = 16$

$16 + 12 - 6 - m = 16$

$m = 6$

Answer -

$3 \rightarrow q$
 $2 \overline{) 7}$
 $\underline{6}$
 $1 \rightarrow r$
 $q \times d + r = \text{divident}$
 $(2)(3) + 1 = 7$

Q7)

when $x = 1$

$$P(1) = (1)^3 - 7(1) + 6$$

$$= 1 - 7 + 6$$

$$P(1) = 0$$

when $x = -2$

$$P(-2) = (-2)^3 - 7(-2) + 6$$

$$P(-2) = 12$$

Hence only 1 is zero of $P(x)$

Q8) Solⁿ

put $x = 2$, $P(x) = 2x^3 + 3x^2 - 11x - 6$

$$P(2) = 2(2)^3 + 3(2)^2 - 11(2) - 6$$

$$= 0$$

now $(x - 2)$

$$\begin{array}{r} 2x^2 + 7x + 3 \\ (x-2) \overline{) 2x^3 + 3x^2 - 11x - 6} \\ \underline{+ 2x^3 - 4x^2} \\ 7x^2 - 11x - 6 \\ \underline{+ 7x^2 - 14x} \\ 3x - 6 \\ \underline{+ 3x - 6} \\ 0 \end{array}$$

$$2x^2 + 7x + 3$$

$$2x(x+3) + 1(x+3)$$

$$(2x+1)(x+3)$$

put $2x+1=0$ $x = -1/2$, $x = -3$ Answer

Hence $2, -3, -1/2$ are zeros of $P(x)$

Q9) $f(x) = x^3 - x^2 - 14x + 8$ in form $f(x) = (x-a)$

Sol: $f(x) = (x-a)q(x) + r$

$q(x) + r$
where $a = 4$

$$x^3 - x^2 - 14x + 8 = (x-4)q(x) + r$$

$$\begin{array}{r} x^2 + 3x - 2 \\ x-4 \overline{) x^3 - x^2 - 14x + 8} \\ \underline{+ x^3 - 4x^2} \\ 3x^2 - 14x + 8 \end{array}$$

$$\begin{array}{r} 3x^2 - 14x + 8 \\ \underline{+ 3x^2 - 12x} \\ -2x + 8 \end{array}$$

Hence

$$(x-4)(x^2 + 3x - 2) + 0$$

$$\begin{array}{r} -2x + 8 \\ \underline{+ 2x - 8} \\ 0 \end{array}$$

$$\begin{array}{r} 4 - a \\ 2 \overline{) 9} \\ \underline{-8} \\ 1 \end{array}$$

divisor

remainder

Q10 Volume = (area of floor) $\times$ (height of room)

$$x^3 + 11x^2 + 34x + 24 = \text{area} \times (x+1)$$

$$\text{area} = \frac{x^3 + 11x^2 + 34x + 24}{x+1}$$

$$\begin{array}{r} x^2 + 10x + 24 \\ x+1 \overline{) x^3 + 11x^2 + 34x + 24} \\ \underline{+ x^3 + x^2} \\ 10x^2 + 34x + 24 \end{array}$$

area of floor

$$= x^2 + 10x + 24$$

Ans

$$\begin{array}{r} 10x^2 + 34x + 24 \\ \underline{+ 10x^2 + 10x} \\ 24x + 24 \end{array}$$

$$\begin{array}{r} 24x + 24 \\ \underline{+ 24x + 24} \\ 48x + 48 \end{array}$$

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